Adding a sequence in the form: 1 + 2 + ... + n:

A. This sequence is sometimes referred to as *Triangular Numbers*, and can be solved by the equation:

$$\sum_{i=1}^{n} i = 1 + 2 + \dots + n = \frac{n \cdot (n+1)}{2}$$

- B. Using numbers instead of variables we get the following:
 - 1. Multiply the last number by that number plus 1, then divide by 2.
 - 2. Notice one of these numbers is divisible by 2, so you can divide the even number by 2 and then multiply by the other number.

Ex [1] 1 + 2 + ... + 10 =_____.

- a) From the equation we know this is equal to: ${}^{10 \text{ x} 11}/_2 \text{ or } 5 \text{ x} 11 = 55$.
- b) The answer is 55.
- Ex [2] 1 + 2 + ... + 50 =_____.
 - a) From the equation we know this is equal to: ${}^{50 \times 51}/_2$ or 25 x 51 = 1275. See <u>Multiplying by 25</u>.
 - b) The answer is 1275.
- C. Sometimes there might be a number missing to throw you off, so you need to be careful.

Ex [3] $2 + 3 + 4 + \dots + 25 =$ _____.

- a) Notice that the number 1 is missing from the equation. Treat it as though it were there.
- b) From the equation we know this is equal to: ${}^{25 \times 26}/_2$ or 25 x 13 = 325.
- c) Since the number 1 is missing, you should subtract 1 from 325. The answer is 324.