

Repeating Decimals In The Form: .abbb..., .abccc..., .abcddd..., etc.

A. To change repeating decimals of this pattern to fractions follow these steps:

1. To find the numerator, take the digits that are NOT repeating and subtract this value from these digits plus one more.
2. The first digit of the denominator is 9 followed by the same number of 0's as the number of non-repeating digits.

Ex [1] $.12333... = \underline{\hspace{2cm}}$ (fraction)

- a. The numerator is $123 - 12 = 111$.
- b. The denominator is 900.
- c. The fraction is $\frac{111}{900}$ which reduces to $\frac{37}{300}$.
- d. The answer is $\frac{37}{300}$.

Ex [2] $.2444... = \underline{\hspace{2cm}}$ (fraction)

- a. The numerator is $24 - 2 = 22$.
- b. The denominator is 90.
- c. The fraction is $\frac{22}{90}$ which reduces to $\frac{11}{45}$.
- d. The answer is $\frac{11}{45}$.

B. If the repeating digit is a 9, then the problem becomes easier:

1. Add 1 to the non repeating digits to get the decimal form of the answer.

Ex [1] $.4999... = \underline{\hspace{2cm}}$ (fraction).

- a. Add 1 to 4 to get 5. The decimal form of the answer is .5. So the answer in a fraction is $\frac{1}{2}$.

Ex [2] $.74999... = \underline{\hspace{2cm}}$ (fraction).

- a. Add 1 to 74 to get 75. The decimal form of the answer is .75. So the answer in a fraction is $\frac{3}{4}$.