

Multiplying Fractions In The Form: $a \times \frac{a}{b}$

A. From algebra we learn:

$$a \times \frac{a}{b} = a - (b - a) + \frac{(b - a)^2}{b}$$

*Note: Since you are squaring $(b - a)$ it does not matter if you use $(b - a)^2$ or $(a - b)^2$

B. Use the following steps:

1. The denominator is always b .
2. Subtract the values b and a and square it. This is the numerator.
3. If the resulting fraction is proper, write it down, otherwise "fix" it and carry.
4. If $\frac{a}{b}$ is proper: subtract the difference of b and a from a to get the whole number.
5. If $\frac{a}{b}$ is improper: add the difference of b and a to a to get the whole number.

Ex [1] $13 \times \frac{13}{15} = \underline{\hspace{2cm}}$ (mixed number).

- a) $(15 - 13)^2 = 4$. This is the numerator.
- b) Since $\frac{4}{15}$ is a proper fraction we write it down.
- c) Since the fraction $\frac{13}{15}$ is proper, we subtract the difference, 2, from 13, which equals 11. This is the whole number.
- d) The answer is $11 \frac{4}{15}$.

Ex [2] $8 \times \frac{8}{5} = \underline{\hspace{2cm}}$ (mixed number).

- a) $(8 - 5)^2 = 9$.
- b) Since $\frac{9}{5}$ is an improper fraction, rewrite it as $1 \frac{4}{5}$. Write $\frac{4}{5}$ and carry the 1.
- c) Since $\frac{8}{5}$ is improper, add the difference, 3, to 8, which equals 11. Adding the carried number the whole number becomes 12.
- d) The answer is $12 \frac{4}{5}$.